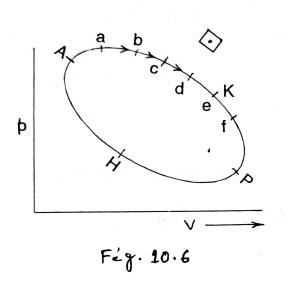
of an isolated system remains constant or increases according as the process is reversible or irreversible  $dS \ge 0$ .

## CLAUSIUS INEQUALITY: PRINCIPLES OF INCREASE OF ENTROPY:

A system passes through a cyclic process which consists of a set of states and finally comes to the initial state to start with. As shown in the figure, the original cyclic process represented as AKPH may be supposed



to consist of large number of small steps represented by ab, bc, cd, de, ef etc, these isothermals are at temperatures  $T_1$ ,  $T_2$ ,  $T_3$ , .......  $T_n$  and larger is the number of steps, better will be the simulation of the original cycle with a set of states on isotherms. Let  $Q_1$ ,  $Q_2$ ,  $Q_3$ , etc be the heat absorbed by the system at these temperatures. Let there be a reservoir at temperature  $T_0$  higher than the highest of  $T_1$ ,  $T_2$ ,  $T_3$ ...... $T_n$ . We will consider n number of Carnot engines between reservoir at  $T_0$  and heat reservoirs at  $T_1$ ,  $T_2$ ,  $T_3$ ....... $T_n$ . These Carnot engines absorb heat  $Q_1^0$ ,  $Q_2^0$ ,  $Q_3^0$ ...... $Q_n^0$  from the reservior at  $T_0$  and reject  $Q_1$ ,  $Q_2$ ,  $Q_3$ ,...... $Q_n$  at the heat reserviors at temperatures  $T_1$ ,  $T_2$ ,  $T_3$ ,...... $T_n$ .

Now, during a cyclic process the amount of work performed is equal to the amount of heat absorbed. Due to operations of the Carnot's engines, the heat

reservoirs at  $T_1$ ,  $T_2$ ,  $T_3$ , ..... $T_n$  do not lose or gain heat, the total heat absorbed from  $T_0$  would be completely converted into work.

Now,  $Q_0 = Q_1^0 + Q_2^0 + Q_3^0 + \dots + Q_n^0$ Because of Carnot operations, we have,

$$\frac{Q_1^o}{T_0} = \frac{Q_1}{T_1} \Longrightarrow Q_1^o = T_0 \left(\frac{Q_1}{T_1}\right)$$

So for all the Carnot engines, we get,

$$Q_o = T_o \left( \frac{Q_1}{T_1} + \frac{Q_2}{T_2} + \dots + \frac{Q_n}{T_n} \right)$$

$$= T_o \sum \frac{Q_i}{T_i}$$

and this is to be completely converted into work. But this is not possible in accordance with Second law. It means that heat  $Q_1^0$ ,  $Q_2^0$ , etc cannot enter the system.

$$Q_o = T_o \sum \frac{Q_i}{T_i} \le 0$$

$$\Rightarrow \sum_{i=1}^{n} \frac{Q_i}{T_i} \leq 0$$

If n is very large, then the above inequality can be written as

$$\sum \frac{dQ_i}{T_i} \le 0$$

$$\Rightarrow \oint \frac{dQ}{T} \le 0.$$

## This is called CLAUSIUS INEQUALITY.

This is cancer an irreversible cycle, the transformation ABC is an irreversible path and the back transformation C to C t Let us from C to A through a reversible process R, C clausius Inequality, from Clausius Inequality,

From Clausier
$$\int_{1}^{C} \left(\frac{dQ}{T}\right)_{I} + \int_{C}^{A} \left(\frac{dQ}{T}\right)_{R} \leq 0.$$

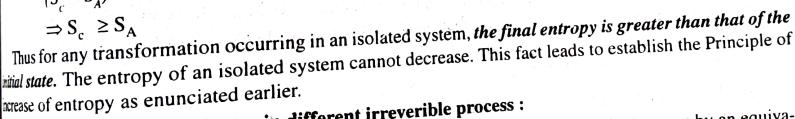
$$\Rightarrow \int_{A}^{C} \left(\frac{dQ}{T}\right)_{I} + (S_{A} - S_{C}) \leq 0$$

$$\Rightarrow \left[\int_{A}^{C} \left(\frac{dQ}{T}\right)_{I} - (S_{C} - S_{A})\right] \leq 0.$$

$$\Rightarrow (S_C - S_A) \ge \int_A^C \left(\frac{dQ}{T}\right)$$

If the system under consideration is isolated (adiabatic), dQ = 0, so

$$(S_c - S_A) = \Delta S \ge 0$$
  
$$\Rightarrow S_c \ge S_A$$



## Calculation of entropy change in different irreverible process:

To calculate the entropy change in an irreversible process we have to replace the process by an equiva-Interversible process by which we reach from a given initial state to a given final state. This is because denotes heat change in irreversible

y which we reach from 
$$dQ = du + dw$$

 $dQ_{\gamma} = du + pdv$  and  $dQ_{i\gamma\gamma} = du + dw$ Where  $dQ_{\gamma}$  denotes heat change in reversible process and  $dQ_{i\gamma\gamma}$ mocess.

Now, for identical state changes.

$$\left(du\right)_{i\gamma}=\left(\mathrm{d}u\right)_{\gamma}$$

$$dQ_{\gamma} = dQ_{i\gamma\gamma} + pdv - dw$$

 $\ln_{\text{Case of reversible process, the second term on the right vanishes because } dw = pdv$  and therefore,

 $dS = \frac{-xr}{T}$ We are to replace the irreversible process by an equivalent reversible path.

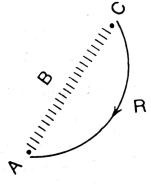


Fig. 10.7